11 a
$$\frac{20-h}{20} = \frac{r}{10}$$

$$10(20 - h) = 20r$$

$$\therefore 200 - 10h = 20r$$

$$\therefore 20 - h = 2r$$

$$\therefore h = 20 - 2r$$
$$= 2(10 - r)$$

$$\mathbf{b} \quad V = \pi r^2 h$$
$$= 2\pi r^2 (10 - r)$$

c Use CAS calculator to solve the equation $2\pi x^2(10 - r) = 500$, given that 0 < r < 10. This gives r = 3.49857... or r = 9.02244...

When
$$r = 3.49857...$$
, $h = 2(10 - 3.49857...)$

When
$$r = 9.02244...$$
, $h = 2(10 - 9.02244...)$

Therefore the volume of the cylinder is 500 cm^3 when r = 3.50 and h = 13.00 or when r = 9.02 and h = 1.96, correct to two decimal places.

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